

Solid State Theory: Band Structure Methods

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Computer room

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Outline:

- **Computing the phonon frequencies of silicon at the Gamma point.**
- **Generating a grid in q space.**
- **Computing the frequencies of silicon on a regular grid.**
- **Obtaining dispersions through Fourier transform of the force constants.**

Silicon:

Table: basic information about and classifications of silicon.

- Name: Silicon
- Symbol: Si
- Atomic number: 14
- Atomic weight: 28.0855 (3) [see note r]
- Standard state: solid at 298 K
- CAS Registry ID: 7440-21-3
- Group in periodic table: 14
- Group name: (none)
- Period in periodic table: 3
- Block in periodic table: p-block
- Colour: dark grey with a bluish tinge
- Classification: Semi-metallic

Space group: $Fd-3m$ (Space group number: 227)

Structure: diamond

Cell parameters:

a : 356.9 pm

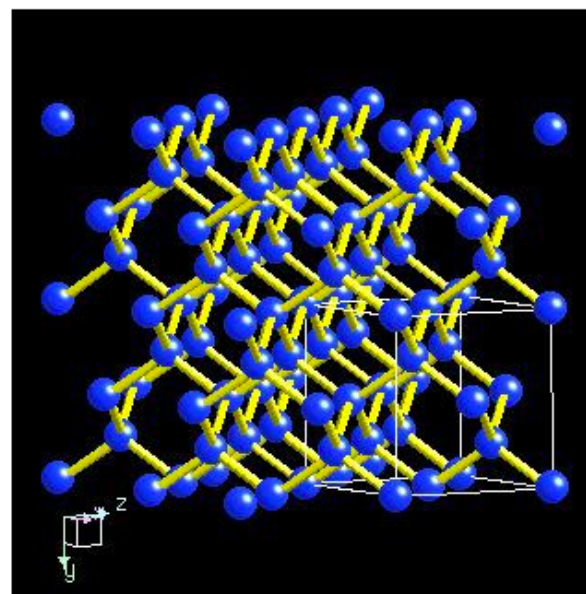
b : 356.9 pm

c : 356.9 pm

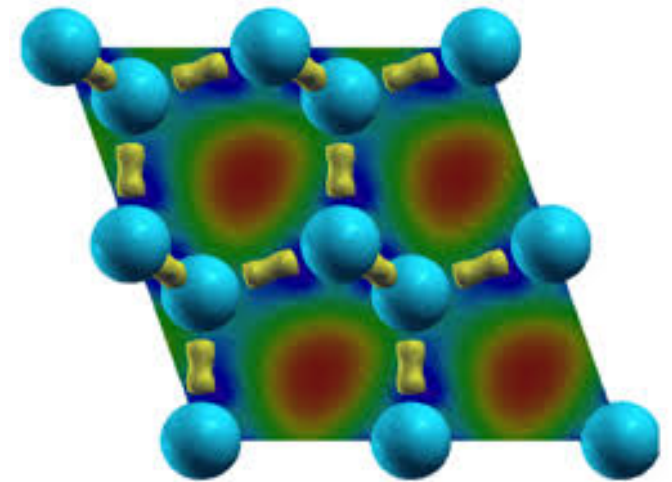
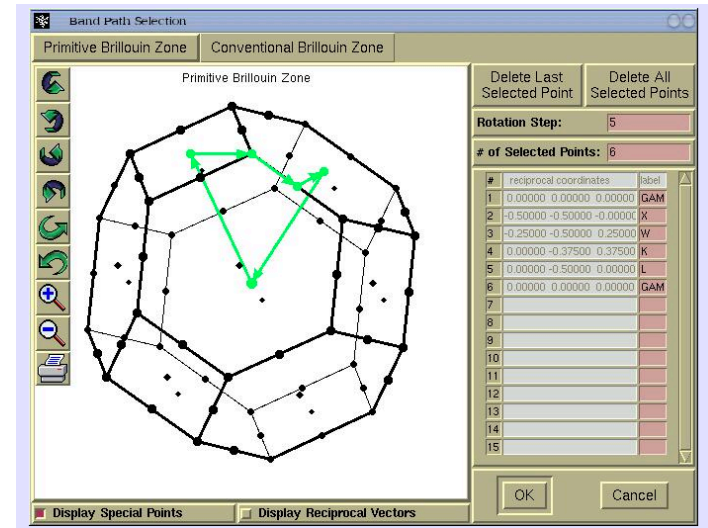
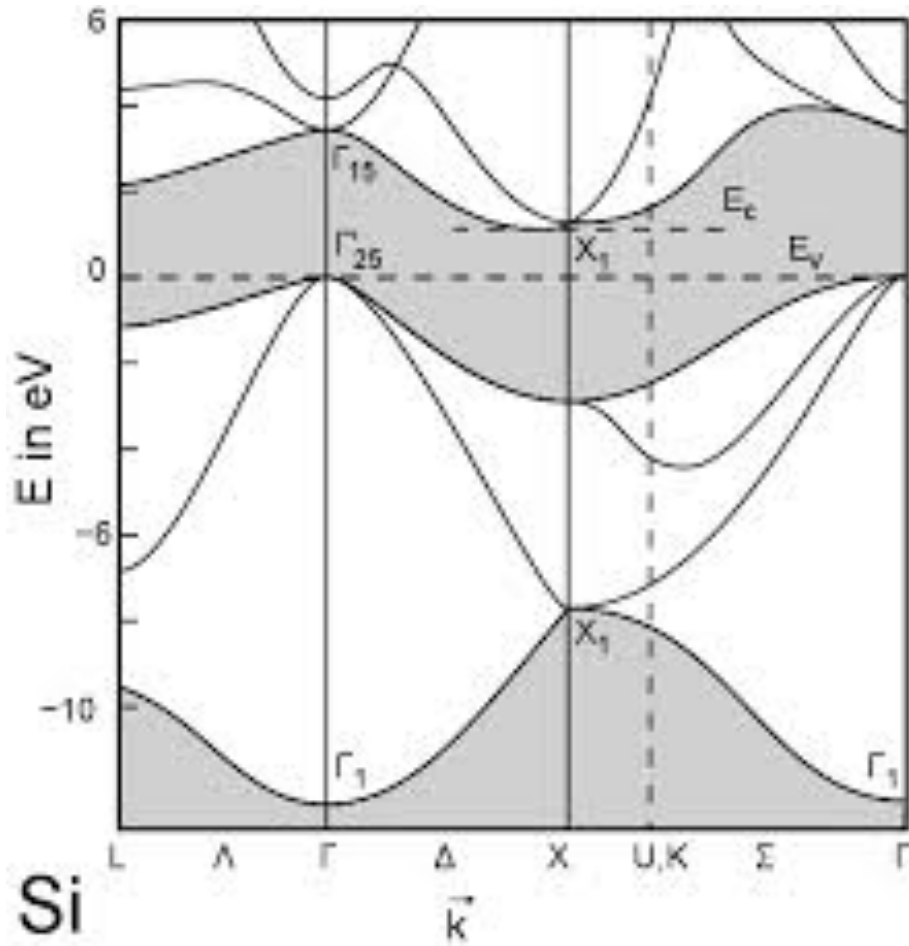
α : 90.000°

β : 90.000°

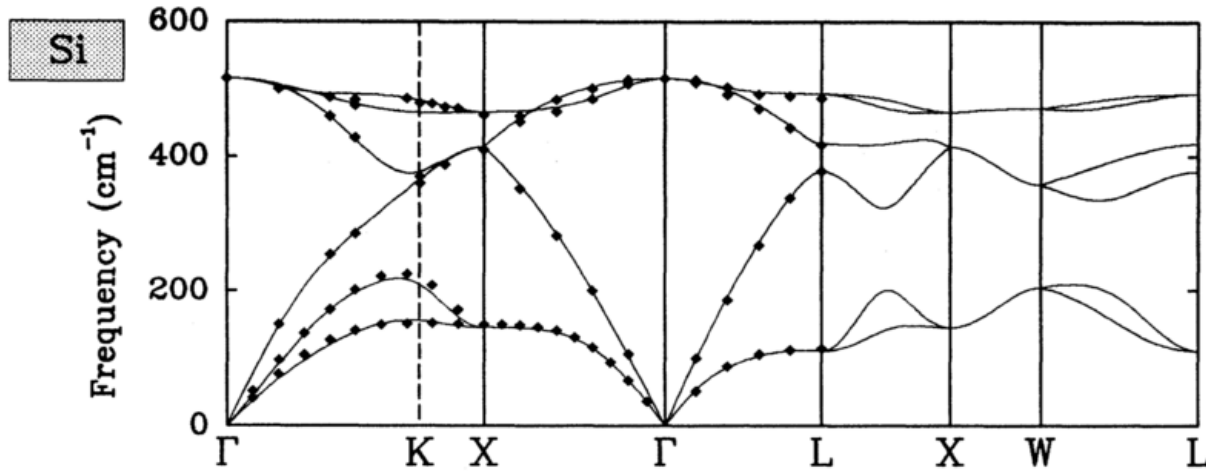
γ : 90.000°



Electronic Structure:



Silicon Phonon Dispersions

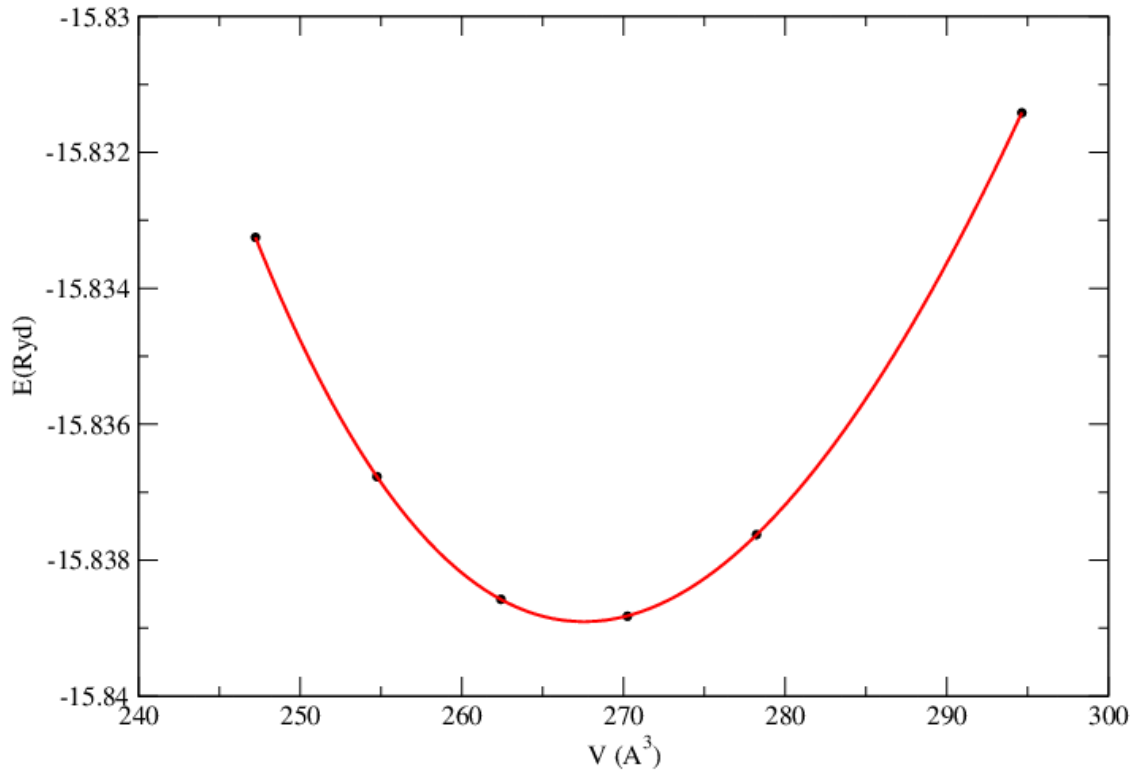


Q point	Ω (THz)
$\Gamma_{LO/TO}$	15.5
X_{TO}	13.9
$X_{LA/TO}$	12.3
X_{TA}	4.5
L_{TO}	14.7
L_{LO}	12.6
L_{LA}	11.4
L_{TA}	3.4

Units:

$$1\text{THz}=33.357\text{ cm}^{-1}=122.65\text{ meV}$$

Equation of state:



Equation of state: EOS2 (PRB52,8064)

a,b,c,d -15.977229 52.489842 -659.228070 2105.431619

$V_0, B(\text{GPa}), B_0, E_0$ 267.5514 94.4139 4.0179

Equation of state: Murnaghan

$V_0, B(\text{GPa}), B_0, E_0$ 267.5519 94.1350 4.0339 -15.838904

Experiment:

$V_0, B(\text{GPa})$: 270.24 97.6

Pressure Behaviour (Grüneisen Parameters):

$$\gamma_i = \frac{B_T}{\omega_i} \frac{\partial \omega_i}{\partial P}$$

Table I. Mode Grüneisen parameter γ_i for Si and Ge.

Γ	Si	Ge	L	Si	Ge
$\gamma_{TO}(=\gamma_{LO})$	1.00 ± 0.06	1.12 ± 0.02	γ_{TO}	1.3 ± 0.2	0.9 ± 0.1
$\gamma_{LA}[1, 0, 0]$	1.110	1.301	γ_{LO}	1.2*	1.2 ± 0.2
$\gamma_{TA}[1, 0, 0]$	0.325	0.612	γ_{LA}	1.0*	0.5 ± 0.1
$\gamma_{LA}[1, 1, 0]$	1.106	1.294	γ_{TA}	-1.3 ± 0.3	-0.4 ± 0.3
$\gamma_{TA1}[1, 1, 0]$	0.325	0.612	X		
$\gamma_{TA2}[1, 1, 0]$	-0.099	0.161	γ_{TO}	1.5 ± 0.1	—
$\gamma_{LA}[1, 1, 1]$	1.105	1.292	$\gamma_{LO}(\approx \gamma_{LA})$	0.9*	—
$\gamma_{TA}[1, 1, 1]$	0.086	0.367	γ_{TA}	-1.4 ± 0.3	—

* These data are adopted as the average value in many theories⁶⁻¹¹⁾ and bring only a little influence on the total Grüneisen constant.

