Activities during last months

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- Global Neoclassical Fluxes with Er≠0
- Electric Field Resonances (ion transport)
- Bootstrap calculations for TJ-II

Neoclassical Global Fluxes





- "The linear drift kinetic equation with or without bounce average is intrinsically incompatible with large orbit size regardless of its fraction"
- "The authors neither solve for the equilibrium distribution function to show that it is a Maxwellian, nor show that the relaxation rate of the plasma profiles is slower than that of the distribution function"
- "The zero order equation for f_0 in linear drift kinetic theory is not valid for large orbits. Thus, using a Maxwellian distribution for f_0 is incorrect"



- What to do **without** the local approach?
 - Under *real* conditions in **real** devices
 - Without really solving the 5D DKE

 $\checkmark \quad Check the local approach with E_r=0 \\ \implies Include electric field effects$









$$\langle \Gamma(\psi, v) \rangle = \langle D^0(\psi, v) \rangle f(\psi, v) + \langle D^1(\psi, v) \rangle \frac{df}{d\psi} + \dots + \langle D^n(\psi, v) \rangle \frac{d^n f}{d\psi^n}$$

$$\langle D^n(\psi, v) \rangle_{p.t} = \frac{(-1)^n}{(n+1)!} \frac{a}{2\sqrt{\psi}} \frac{1}{N_p N_t} \sum_{i=1}^{N_p} \sum_{j=1}^{N_t} \frac{\psi_j - \psi_{j-1}}{t_j - t_{j-1}} (\psi_j - \psi_{j-1})^n$$



- Dealing with the radial electric field
 - Kinetic energy is not conserved
 - Monoenergetic approach dubious
 - Appearance of electrostatic barriers
 - Ambipolarity becomes highly non linear
- Compute fluxes for the local ambipolar Er





$$\Gamma^{n}(\psi) = \frac{4}{\sqrt{\pi}} \int_{0}^{\infty} \langle D^{n}(\psi, v) \rangle_{p,t} \left(\nabla_{\psi} \right) f_{Max}(\psi, v) v^{2} dv = -\langle D^{n}(\psi) \rangle_{v}(\nabla_{\psi})$$

Kinetic energy is not conserved Monoenergetic approach acceptable



2

1.5

1

D₀



Appearance of electrostatic barriers funny trajectories





TJ-II



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TJ-II



Electric Field Resonances



Electric Field Resonances







In the monoenergetic approach resonances appears at high values due to TJ-II's high iota (0.9 < 1 < 2.2)

$$E_{res} = \iota v B \frac{r}{R}$$

However for low density ECRH plasmas E_r can be very high, and Ti very low.



TJ-II at r/a = 0.5



 $|E|/vB_0 = 3 \times 10^{-3}, 1 \times 10^{-3}, 3 \times 10^{-4}, 1 \times 10^{-4}, 3 \times 10^{-5}$ and zero.

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The neural network method, in a first attempt, does not work very well for these kind of behaviors

What is your experience?

Is it possible to incorporate resonances into Craig's formalism ?

Bootstrap Currents in TJ-II



Bootstrap in TJ-II



DKES (borrowed from Henning)



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Convolutions



$$L_{1j} = \frac{4}{\sqrt{\pi}} \int_0^\infty D_{11}^* \left(\frac{r}{a}, \frac{\nu}{v}, \frac{E_r}{vB}\right) \left(\frac{v}{v_{th}}\right)^{2j} exp\left[-\left(\frac{v}{v_{th}}\right)^2\right] \frac{dv}{v_{th}} \qquad L_{j3} = G_b \frac{4}{\sqrt{\pi}} \int_0^\infty D_{13}^* \left(\frac{r}{a}, \frac{\nu}{v}, \frac{E_r}{vB}\right) \left(\frac{v}{v_{th}}\right)^{2(j+1)} exp\left[-\left(\frac{v}{v_{th}}\right)^2\right] \frac{dv}{v_{th}} \qquad L_{j3} = G_b \frac{4}{\sqrt{\pi}} \int_0^\infty D_{13}^* \left(\frac{r}{a}, \frac{\nu}{v}, \frac{E_r}{vB}\right) \left(\frac{v}{v_{th}}\right)^{2(j+1)} exp\left[-\left(\frac{v}{v_{th}}\right)^2\right] \frac{dv}{v_{th}} \qquad L_{j3} = G_b \frac{4}{\sqrt{\pi}} \int_0^\infty D_{13}^* \left(\frac{r}{a}, \frac{\nu}{v}, \frac{E_r}{vB}\right) \left(\frac{v}{v_{th}}\right)^{2(j+1)} exp\left[-\left(\frac{v}{v_{th}}\right)^2\right] \frac{dv}{v_{th}} \qquad L_{j3} = G_b \frac{4}{\sqrt{\pi}} \int_0^\infty D_{13}^* \left(\frac{r}{a}, \frac{\nu}{v}, \frac{E_r}{vB}\right) \left(\frac{v}{v_{th}}\right)^{2(j+1)} exp\left[-\left(\frac{v}{v_{th}}\right)^2\right] \frac{dv}{v_{th}} \qquad L_{j3} = G_b \frac{4}{\sqrt{\pi}} \int_0^\infty D_{13}^* \left(\frac{r}{a}, \frac{v}{v}, \frac{E_r}{vB}\right) \left(\frac{v}{v_{th}}\right)^{2(j+1)} exp\left[-\left(\frac{v}{v_{th}}\right)^2\right] \frac{dv}{v_{th}} \qquad L_{j3} = G_b \frac{4}{\sqrt{\pi}} \int_0^\infty D_{13}^* \left(\frac{r}{a}, \frac{v}{v}, \frac{E_r}{vB}\right) \left(\frac{v}{v_{th}}\right)^{2(j+1)} exp\left[-\left(\frac{v}{v_{th}}\right)^2\right] \frac{dv}{v_{th}} \qquad L_{j3} = G_b \frac{4}{\sqrt{\pi}} \int_0^\infty D_{13}^* \left(\frac{r}{a}, \frac{v}{v}, \frac{E_r}{vB}\right) \left(\frac{v}{v_{th}}\right)^{2(j+1)} exp\left[-\left(\frac{v}{v_{th}}\right)^2\right] \frac{dv}{v_{th}} \qquad L_{j3} = G_b \frac{4}{\sqrt{\pi}} \int_0^\infty D_{13}^* \left(\frac{r}{a}, \frac{v}{v}, \frac{E_r}{vB}\right) \left(\frac{v}{v_{th}}\right)^{2(j+1)} exp\left[-\left(\frac{v}{v_{th}}\right)^2\right] \frac{dv}{v_{th}} \qquad L_{j3} = G_b \frac{4}{\sqrt{\pi}} \int_0^\infty D_{13}^* \left(\frac{r}{a}, \frac{v}{v}, \frac{E_r}{vB}\right) \left(\frac{v}{v_{th}}\right)^{2(j+1)} exp\left[-\left(\frac{v}{v_{th}}\right)^2\right] \frac{dv}{v_{th}} \qquad L_{j4} = G_b \frac{4}{\sqrt{\pi}} \int_0^\infty D_{13}^* \left(\frac{r}{a}, \frac{v}{v}, \frac{E_r}{vB}\right) \left(\frac{v}{v_{th}}\right)^{2(j+1)} exp\left[-\left(\frac{v}{v_{th}}\right)^2\right] \frac{dv}{v_{th}} \qquad L_{j4} = G_b \frac{4}{\sqrt{\pi}} \int_0^\infty D_{13}^* \left(\frac{r}{a}, \frac{v}{v}, \frac{E_r}{vB}\right) \frac{dv}{v_{th}} \frac{dv}{v_{th}} = G_b \frac{4}{\sqrt{\pi}} \int_0^\infty D_{13}^* exp\left[-\left(\frac{v}{v_{th}}\right)^2\right] \frac{dv}{v_{th}} \frac{dv}{$$



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Results





Results





Results $\Delta \iota(r) \approx \frac{R\mu_0}{Br^2} \int_0^r r' j_{\parallel}(r') dr'$ $dI = \int_0^r j_{\parallel} dS \approx 2\pi \int_0^r r' j_{\parallel}(r') dr'$ 30 7 $E_{r} = 0$ E = 025 6 vacuum r with bootstrap 5 20 dI (kA) 15 4 10 3 2 5 0 1.7 1000 $E_r \neq 0$ vacuum 500 with bootstrap 1.65 dI (A) 0 1.6 _ -500 1.55 -1000 1.5 10 12 14 12 8 16 10 14 16 0 2 0 2 4 6 8 Δ 6 r (cm) r (cm)

Future



- Global Fluxes
 - Publish the results (not successful so far)
- E_r resonances
 - Ion transport
- Bootstrap currents
 - Run DKES to account for the ambipolar $E_{\rm r}$ and r/a
 - Systematic error analysis
- Who can predict the future ?